# A Survey of Verifiable Delegation of Computations

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Outline •	Motivation	Verifiable Computation	Memory Delegation	Conclusion O
Talk Our	tline			

### Motivation

Cloud computing, Small Devices, Large Scale Computation

## Generic Results for Verifiable Computation

### Protocols that work for arbitrary computations

- Interactive Proofs
- Probabilistically Checkable Proofs
- "Muggles" Proofs
- Other Arithmetizations approaches (QSP)
- Implementations (Pinocchio, Snark-for-C)

#### Delegation of Memory

- Homomorphic MACs
- Proofs of Retrievability
- Verifiable Keyword Search

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Computin	g on Demand	1		

## **Cloud Computing**

Businesses buy computing power from a service provider

#### Advantages

- No need to provision and maintain hardware
- Pay for what you need
- Easily and quickly scalable up or down

### Trust Issues

- Transfer possibly confidential data to computing service provider
- Trust computation is performed correctly without errors
- Malicious or benign

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Small E	Devices			

- Small devices outsourcing complex computing problems to larger servers
  - Photo manipulations
  - Cryptographic operations
- Same issues:
  - Confidentiality of data
  - Correctness of result



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Large S	Scale Comput	ations		

- Network-based computations
  - SETI@Home
  - Folding@Home
- Users donate idle cycles
  - Known problem: users return fake results without performing the computation
  - Increases their ranking
- Needed a way to efficiently weed out bad results
  - Currently use redundancy



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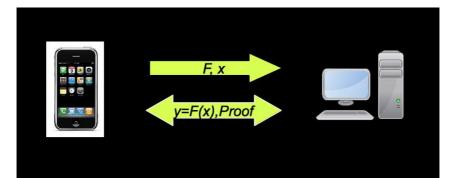
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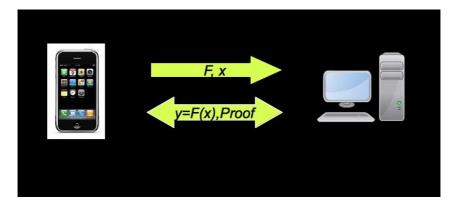
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Verifiabl	e Computati	ion		

- $\blacksquare$  The client sends a function F and an input x to the server
- The server returns y = F(x) and a proof  $\Pi$  that y is correct. Verifying  $\Pi$  should take less time than computing F.



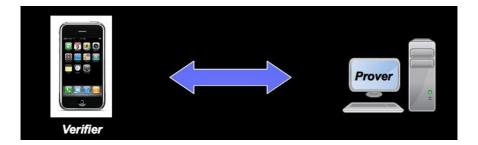
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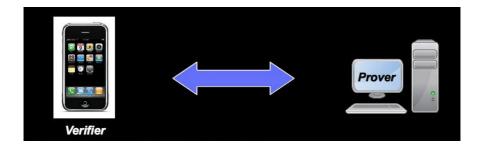
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Interactive	e Proofs (GN	1R,B)		

- An all powerful Prover interacts with a poly-time Verifier
  - Prover convinces Verifier of a statement she cannot decide on her own
  - Probabilist guarantee
  - All of PSPACE can be proven this way [LFKN,S]
- We want something different
  - A scaled back version of this protocols for efficient computations
  - A powerful but still efficient prover: its complexity should be as close as possible to the original computation
  - A super-efficient Verifier: ideally linear time



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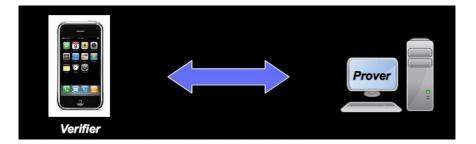
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Muggles F	Proofs (GKR)			

Poly-time Prover interacts with a quasi-linear Verifier

Refines the proof that IP=PSPACE to efficient computations

 $\blacksquare$  For a log-space uniform NC circuit of depth d

- Prover runs in poly(n)
- Verifier runs in O(n + poly(d))
- Interactive  $(O(d \cdot \log n) \text{ rounds})$
- Unconditional Soundness

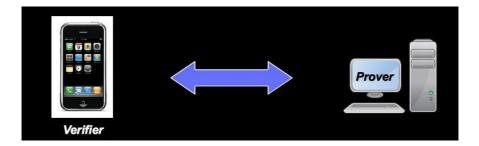


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Optimiza	ations and Ir	nplementations (CN	ЛТ,Т)	

## $\blacksquare$ Prover can be implemented in $O(S\log S)$

- $\hfill\blacksquare$  Where S is the size of the circuit computing the function
- $\hfill O(S)$  for circuits with a regular wiring pattern
- Implementation tests show that for the regular wiring pattern case the prover is less than 10x slower than simply computing the function.

## Protocol remains highly interactive

Interaction can be removed via the Fiat-Shamir heuristic (random oracle model).



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Probabilist	cically Checka	able Proofs		

- The IP=PSPACE result yielded a surprising consequence: any computation can be associated with a (very long) proof which can be queried in only a constant number of locations (...AMLSS, AS, ...)
- The Prover commits to this proof using a Merkle tree and then the Verifier queries it and verifies the openings (K)
  - Note that now we have an *argument* with a computational soundness guarantee
- This protocol can also be made non-interactive using the random oracle (M) or strong extractability assumptions about the hash function used in the protocol (DL,BCCT,GLR)
- Main bottleneck: still the Prover's complexity  $O(S^{1.5})$

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- Turn a circuit computation into a set of polynomial equations
  - Replace each gate with a quadratic polynomial
  - Check these polynomial identities in a randomized fashion by checking them on random points
  - Use error-correcting encodings to make sure that the proof is *locally* checkable (i.e. to reduce the number of random queries to the proof)

### Can we use different arithmetizations?

- Avoid composing long PCP proofs with compressing hash functions for a more direct way to get short proofs
- Linear Prover complexity?
- Groth showed a different approach
  - Polynomial equations are verified in the exponent (using bilinear maps over a cyclic group)
  - A Diffie-Hellman type of assumption prevents the Prover from cheating
  - Proof is very compact without using Merkle trees
  - Drawback: quadratic prover complexity and a quadratic CRS
  - Lipmaa shows how to reduce those to quasilinear

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Quadrati	c Span Prog	grams (GGPR)		

- To check that all the wires in the circuits are correct it just requires a linear test (*span program*)
- This would be too much work for the verifier (same as the size of the circuit)
- Build two copies of the "checking" span program and test them against each other
- = A QSP is defined by two sets of polynomials  $V = \{v_1, ..., v_{n+m}\}$ ,  $W = \{v_1, ..., v_{n+m}\}$  and a target polynomial t
  - We say that a QSP (V,W,t) computes a Boolean function *P* of *n* inputs if and only if
  - For all  $x = (x_1 \dots x_n)$  s.t. F(x) = 1
  - $\pi$  it divides the product of a linear combination of subsets of V and W
    - $= t \left( \Sigma_{i=1}^{n} a_i v_i \right) \cdot \left( \Sigma_{i=1}^{n} b_i v_i \right)$
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The QSP	protocol			

In a preprocessing stage the Verifier publishes the values  $g^{s^i},\,g^{v_i(s)},\,g^{w_i(s)}$  and  $g^{t(s)}$ 

### • for a secret random value s.

 $\blacksquare$  On input x the server finds the coefficients  $a_i,\,b_i$  and polynomial h such that

 $\bullet t \cdot h = (\sum_{i=1}^{n} a_i v_i) \cdot (\sum_{i=1}^{n} b_i w_i)$ 

Using the values produced by the Verifier the Prover can evaluate in the exponent the above equation at the point s

Verifier checks the equation using bilinear maps

- Efficiency:
  - The verifier is linear to prepare the input; constant time to verify the result
  - Prover is quasi-linear the polylog overhead comes from doing polynomial division to compute h
- Security: requires a Diffie-Hellman type of assumption which assumes that the prover cannot divide in the exponent.

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- $\blacksquare$  On input x the server finds the coefficients  $a_i, \, b_i$  and polynomial h such that

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Implement	ation Results	;		

An end-to-end toolchain that compiles a subset of C into QSPs

- Proof size is 288 bytes regardless of what it is being computed
- Verification time is 10ms
- Prover complexity still not quite there in practice
  - About 60 times faster than previous proposals
  - Can run some lightweight computations

## SNARKs-for-C (BCGTV)

Given a C program, they produce a circuit whose satisfiability encodesses the correctness of execution of the program.

First the C program is compiled into machine code for TinyRAM

Then the TimyRam code is compiled into a circuit

A QSP is built for this circuit.

Use the generic concept of Linear Interactive Proof.

could plug a more efficient LIP if one is found

Slightly less efficient for the Verifier

Proof size 322 bytes

Verification time dependent on *x* (from 103ms to 5s for long inputs) A bit more efficient for the Prover

Were able to handle a Traveling Salesman Decider on a 200-nodes

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Impleme	Implementation Results					

- An end-to-end toolchain that compiles a subset of C into QSPs
- Proof size is 288 bytes regardless of what it is being computed

#### Verification time is 10ms

- Prover complexity still not quite there in practice
  - About 60 times faster than previous proposals
  - Can run some lightweight computations

- Given a C program, they produce a circuit whose satisfiability encodes the correctness of execution of the program.
  - First the C program is compiled into machine code for TinyRAM.
  - Then the TimyRam code is compiled into a circuit
  - A QSP is built for this circuit.
    - Use the generic concept of Linear Interactive Proof
    - sould plug a more efficient LIP if one is found
  - Slightly less efficient for the Verifier
    - Proof size 322 bytes
  - Verification time dependent on a (from 108ms to 5s for long inputs) A bit more efficient for the Prover
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  - Client's limitation is in computing time
  - $\blacksquare$  Cannot compute F on its own
- What if the client's limitation is *storage*?
  - $\blacksquare$  Client stores large quantity of data D with the server
  - later queries F on D and receives back F(D)
- Previous approaches do not work: they require the client to know the input

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  - $\blacksquare$  Client only stores the short key k
- Later the client submits F
  - Server returns y = F(D) and t
  - Client accepts if and only if  $t = MAC_k(y)$
  - $\blacksquare$  Verification time may be as long as computing F focus on storage and bandwidth
- Original idea uses homomorphic encryption
  - Mostly of theoretical interest
- New ideas use "traditional" crypto (CF,GN)
  - Much more efficient
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Proofs o	of Retrievabil	ity (JK)		

- Client stores a large file F with the server and wants to make sure that it can be retrieved without downloading the entire thing (e.g. auditing)
  - $\blacksquare$  Client sends a short  $\mathit{challenge}\ c$
  - $\blacksquare$  Server responds with a short answer a
    - avoid reading the entire file to produce the answer
- A possible solution (A+,SW)
  - Encode the file F using an error correcting code F' = Encode(F)
  - Store each block  $F'_i$  with a *linearly homomorphic* MAC  $t_i = MAC_k(F'_i)$
  - The client queries a small number  $(\ell)$  of the blocks  $F_{i_1} \dots F_{i_\ell}$  and also sends  $\ell$  random coefficients  $\lambda_1, \dots, \lambda_\ell$
  - $\blacksquare$  The server sends back  $\phi = \Sigma_j \lambda_j F_{i_j}$  and  $t = \Sigma_j \lambda_j t_j$
  - The client accepts if and only if  $t = MAC_k(\phi)$
- The scheme is very efficient
  - Linearly homomorphic MACs can be built from basic universal hash functions
  - Minimal storage overhead due to the error-correction expansion
  - Query complexity is quadratic in the security parameter

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Verifiab	le Keyword S	earch (BGV)		

- Client stores a large text file  $F = w_1, \ldots, w_n$  with the server
  - $\blacksquare$  Client sends a keyword w
  - Server responds with yes/no
  - how can we efficiently verify the answer?
- Encode the file as the polynomial F(X) = Π<sub>i</sub>(X − w<sub>i</sub>)
   Note that F(w) = 0 if and only if w ∈ F
- Problem reduces to efficiently verifying the computation of a large degree polynomial.



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Verifiable	Computation	of Polynomials	(BGV)	

#### • Other applications besides Verifiable Keyword Search

- Client stores a high degree polynomial  $F(X) = \Sigma a_i X^i$ 
  - Client sends a value x
  - Server responds y = F(x)
  - how can we efficiently verify the answer?

Store the MAC  $t_i = ca_i + r_i$ 

- $r_i$  are computed pseudorandomly, i.e.  $r_i = PRF_k(i)$
- Client only stores random secret keys c, k
- Let R(X) be the polynomial defined by the  $r_i$
- When the client queries the value x, the server returns
   y = Σ<sub>i</sub>a<sub>i</sub>x<sup>i</sup> and t = Σ<sub>i</sub>t<sub>i</sub>x<sup>i</sup>
- The client checks that t = cy + R(x)
  - Note that this requires O(d) work where d is the degree of the poly
  - This can be reduced if we use *closed-form efficient* PRFs
  - Knowledge of the key k allows the computation of  $\Sigma_i r_i x^i$  in o(d) time
  - We know how to build them from Diffie-Hellman type of assumptions

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Dynamic S	Storage			

- A very important problem is how to deal with updates on the memory
  - without changing the secret state of the client, the server can always ignore updates
  - challenge: updates that do not require the client to re-authenticate large part of the server storage
- Merkle-trees allow to check individual memory locations which change over time
  - but not "global" verifications (proof of retrievability, verifiable keyword search)

Some progress on dynamic proofs of retrievability (CW,SSP)

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  - Protect information from the other clients
  - Becomes secure multiparty computation with an added constraint
    - only one party has enough resources to compute the desired functionality
  - Leverage successes in SMC.
- General VC: Explore more realistic models of computation

e.g. RAM

Explore more pragmatic approaches

- Weaker security guarantee that rules out most likely forms of attacks e.g. program checking against bugs in the implementation
- Does the outsourcing of polynomials have larger applicability?
  - Alternatively, can we use the same idea of "closed form efficient" PRFs for other computations
- A more efficient general result for memory outsourcing/homomorphic MACs
- "Important" Computations, which would benefit from being outsourced:
  - Image processing
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Future Di	irections			

- Multiple clients
  - Protect information from the other clients
  - Becomes secure multiparty computation with an added constraint
    - only one party has enough resources to compute the desired functionality
  - Leverage successes in SMC.
- General VC: Explore more realistic models of computation
  - e.g. RAM
- Explore more pragmatic approaches
  - Weaker security guarantee that rules out most likely forms of attacks e.g. program checking against bugs in the implementation
- Does the outsourcing of polynomials have larger applicability?
  - Alternatively, can we use the same idea of "closed form efficient" PRFs for other computations
- A more efficient general result for memory outsourcing/homomorphic MACs
- "Important" Computations, which would benefit from being outsourced:
  - Image processing
  - crypto operations